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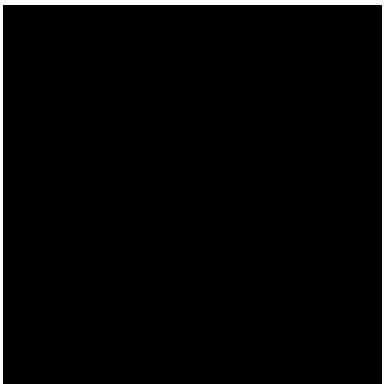
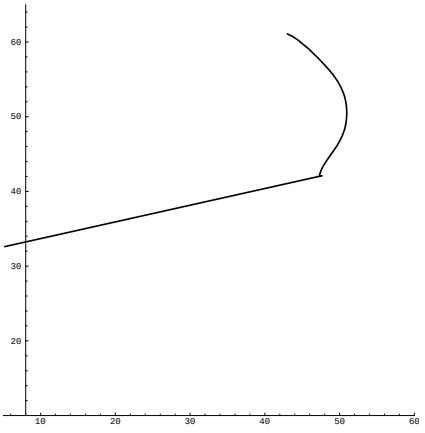


Original Canine Heart MRI Image

Blow Up of the Left Ventricle

Boundary of Left Ventricle



Original Contour

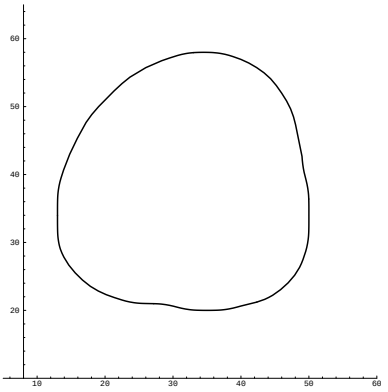


Figure 6. Smoothed Canine Left Ventricle Signatures

Figure 7. The Baer Jigsaw Puzzle