

## Citation for Julian Sahasrabudhe (Whitehead Prize)

### Short citation

Dr Julian Sahasrabudhe of the University of Cambridge is awarded a Whitehead Prize for his outstanding contributions to Ramsey theory, his solutions to famous problems in complex analysis and random matrix theory, and his remarkable progress on sphere packings.

### Long citation

Dr Julian Sahasrabudhe of the University of Cambridge is awarded a Whitehead Prize for his remarkable contributions to several areas of mathematics, including sphere packings, random matrices, complex analysis and Ramsey theory. His work has changed the landscape in each of these areas. His results are characterised by the mostA A bh h H~ efore.

for cosine polynomials. He has solved  
of roots of cosine polynomials such as  $\cos$

$1x + \cos a_2x + \dots + \cos a_nx$  must go to infinity as the number of terms  $n$  increases. This problem had been open for 50 years, and had attracted a lot of attention. He gives a lower bound (in fact, an explicit lower bound) on the number of roots: asrabudhe succeeds in this. A remarkable and unexpected fact: that they must 'correlate' with some easier-to-analyse functions.

Sahasrabudhe has also worked in complex analysis, on Littlewood polynomials. He has solved what was undoubtedly the biggest open problem in this area, a famous problem of Littlewood that asks if there are polynomials of degree  $n$ , with all coefficients  $\pm 1$ , such that the image of the unit circle is bounded both above and below by a multiple of  $n$

polynomials are  
Indeed, computer search

wer bound. The usual belief has been that flat Littlewood polynomials do not exist.

1/2. Such

Sahasrabudhe solves the problem. In joint work with Balister, Bollobás, Morris and Tiba he shows that, in fact, flat Littlewood polynomials do exist. The proof is an amazing and intricate blend of hard analysis (properties of particular trigonometric polynomials) and discrepancy theory.

Recently, Sahasrabudhe has returned to Ramsey theory. He has given the first exponential improvement on the Ramsey numbers  $R(s)$  in over 70 years. It was known that the Ramsey numbers grow at a rate that is at most  $4^s$ , but nobody could improve on the '4'. This has been perhaps the central problem in all of Ramsey theory. Sahasrabudhe, in joint work with Campos, Griffiths and Morris, gives an upper bound of  $(4 - \epsilon)^s$  for a fixed positive constant  $\epsilon$ .

Sahasrabudhe has also made extraordinary progress on sphere packings in high dimensions. The sphere packing problem asks for the densest packing of unit spheres in  $n$